Wolfram Kahl · Michael Winter José N. Oliveira (Eds.)

# Relational and Algebraic Methods in Computer Science

15th International Conference, RAMiCS 2015 Braga, Portugal, September 28 – October 1, 2015 Proceedings



*Editors* Wolfram Kahl McMaster University Hamilton, Ontario Canada

Michael Winter Brock University St. Catharines, Ontario Canada José N. Oliveira Universidade do Minho Braga Portugal

ISSN 0302-9743 Lecture Notes in Computer Science ISBN 978-3-319-24703-8 DOI 10.1007/978-3-319-24704-5 ISSN 1611-3349 (electronic) ISBN 978-3-319-24704-5 (eBook)

Library of Congress Control Number: 2015949476

LNCS Sublibrary: SL1 - Theoretical Computer Science and General Issues

Springer Cham Heidelberg New York Dordrecht London

© Springer International Publishing Switzerland 2015

This work is subject to copyright. All rights are reserved by the Publisher, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, reuse of illustrations, recitation, broadcasting, reproduction on microfilms or in any other physical way, and transmission or information storage and retrieval, electronic adaptation, computer software, or by similar or dissimilar methodology now known or hereafter developed.

The use of general descriptive names, registered names, trademarks, service marks, etc. in this publication does not imply, even in the absence of a specific statement, that such names are exempt from the relevant protective laws and regulations and therefore free for general use.

The publisher, the authors and the editors are safe to assume that the advice and information in this book are believed to be true and accurate at the date of publication. Neither the publisher nor the authors or the editors give a warranty, express or implied, with respect to the material contained herein or for any errors or omissions that may have been made.

Printed on acid-free paper

Springer International Publishing AG Switzerland is part of Springer Science+Business Media (www.springer.com)

# Preface

Relations and formal languages are omnipresent in computer science and in software design. While quantifier-oriented (first- or higher-)order logics can be used to specify and reason about relations, this "element-level style" often obfuscates the structure of specifications and makes reasoning harder. A useful analogy is to consider how element-level reasoning gives way to matrix-level calculations in linear algebra. Similarly, *relation algebra* allows for calculational, largely quantifier-free reasoning about relations, and shares a large subtheory with *Kleene algebra*, the mathematical theory of the regular expressions used for the specification of certain formal languages.

An international collaboration to establish a conference series as a forum for the use of relational methods in computer science, RelMiCS, was initiated during the "38th Banach Semester on Algebraic Methods in Logic and their Computer Science Application" in Warsaw, Poland, September and October 1991. Adapting essentially a one-and-a-half year rhythm, the first 11 RelMiCS conferences were held from 1994 to 2009 on all inhabited continents except Australia. Starting with RelMiCS 7, these were were held as joint events with "Applications of Kleene Algebras" (AKA) conferences. At RelMiCS 11 / AKA 6 in Doha, Qatar, it was decided to continue the series under the unifying name "Relational and Algebraic Methods in Computer Science (RAMiCS)." The next events, RAMiCS 12–14, were then held in Rotterdam, The Netherlands, in 2011, Cambridge, UK, in 2012 and Marienstatt, Germany, in 2014.

This volume contains the proceedings of the 15th International Conference on Relational and Algebraic Methods in Computer Science (RAMiCS 2015), held in Braga, Portugal, from September 28 to October 1, 2015, exactly 24 years after the Banach Semester that resulted in founding this conference series.

The call for papers invited submissions about the theory of relation algebras and Kleene algebras, process algebras, fixed point calculi, idempotent semirings, quantales, allegories, and dynamic algebras, and cylindric algebras, and about their applications in areas such as verification, analysis and development of programs and algorithms, algebraic approaches to logics of programs, modal and dynamic logics, interval and temporal logics, etc.

We were fortunate to be able to invite Gheorghe Stefanescu and Ian Hodkinson who, with their presentations on "A Quest for Kleene Algebra in 2 Dimensions" and "Connections Between Relation Algebras and Cylindric Algebras", nicely emphasized the two traditional theoretical pillars of the RAMiCS conferences, and Ernst-Erich Doberkat, whose presentation "Towards a Probabilistic Interpretation of Game Logic," opened up new opportunities related to modal logic.

The body of this volume is made up of invited papers accompanying these three invited talks, and of 20 contributions by researchers from around the world The papers have been arranged into three groups:

## **Theoretical Foundations**

Including studies of relation-algebraic theories ranging from nominal Kleene algebra to allegories and covering a range of relation concepts, including multirelations, *n*-ary relations, and relational resource semantics

## **Reasoning About Computations and Programs**

With contributions addressing refinement, type checking, and verified relationand Kleene-algebraic programming

#### Applications of Relational and Algebraic Methods

Including to fuzzy databases, rough set theory, preferences, optimization, and text categorization

The contributed papers were selected by the Program Committee from 25 relevant submissions. Each submission was reviewed by at least three Program Committee members; the Program Committee did not meet in person, but had over one week of intense electronic discussions.

We are very grateful to the members of the Program Committee and the subreviewers for their care and diligence in reviewing the submitted papers. We would like to thank the members of the RAMiCS Steering Committee for their support and advice especially in the early phases of the conference organization. We are grateful to INESC TEC and the University of Minho for generously providing administrative support, and we gratefully appreciate the excellent facilities offered by the EasyChair conference administration system. Last but not least, we thank FCT (Fundação para a Ciência e a Tecnologia, Portugal) for their financial support.

July 2015

Wolfram Kahl Michael Winter José N. Oliveira

# Organization

# **Organizing Committee**

## **Conference Chair**

José N. Oliveira

#### **Program Co-chairs**

Wolfram Kahl Michael Winter

Luís S. Barbosa

Manuel A. Cunha

António N. Ribeiro

#### Local Organizers

University of Minho, Portugal University of Minho, Portugal

Brock University, Canada

University of Minho, Portugal

University of Minho, Portugal

McMaster University, Canada

## **Program Committee**

Rudolf Berghammer

Jules Desharnais Marcelo Frias Hitoshi Furusawa Steven Givant Timothy G. Griffin Walter Guttmann Robin Hirsch Peter Höfner Ali Jaoua Peter Jipsen Wolfram Kahl Roger Maddux Ali Mili Bernhard Möller Martin E. Müller José N. Oliveira

Christian-Albrechts-Universität zu Kiel, Germany Université Laval, Canada University of Buenos Aires, Argentina Kagoshima University, Japan Mills College, USA University of Cambridge, UK University of Canterbury, New Zealand University College of London, UK NICTA Ltd., Australia Qatar University, Qatar Chapman University, USA McMaster University, Canada Iowa State University, USA Tunis, Tunisia; NJIT, USA Universität Augsburg, Germany Universität Augsburg, Germany Universidade do Minho, Portugal

#### VIII Organization

Ewa Orłowska	National Institute of Telecommunications, Poland
Agnieszka Rusinowska	Université Paris 1, France
Gunther Schmidt	Universität der Bundeswehr München,
	Germany
Renate Schmidt	University of Manchester, UK
Isar Stubbe	Université du Littoral-Côte-d'Opale, France
Michael Winter	Brock University, Canada

## **Steering Committee**

Rudolf Berghammer Christian-Albrechts-Universität zu Kiel, Germany Jules Desharnais Université Laval, Canada Ali Jaoua Qatar University, Qatar Peter Jipsen Chapman University, USA Bernhard Möller Universität Augsburg, Germany José N. Oliveira Universidade do Minho, Portugal Ewa Orłowska National Institute of Telecommunications, Poland Gunther Schmidt Universität der Bundeswehr München, Germany Michael Winter Brock University, Canada

## **Additional Reviewers**

Ernst-Erich Doberkat Alexander Kurz Annabelle McIver Koki Nishizawa Patrick Roocks Agnieszka Rusinowska Alberto Simões John Stell Insa Stucke Toshinori Takai Norihiro Tsumagari

## **Sponsoring Institutions**

INESC TEC Universidade do Minho FCT (Fundação para a Ciência e a Tecnologia, Portugal)

# Contents

# **Invited Papers**

A Quest for Kleene Algebra in 2 Dimensions Gheorghe Stefanescu	3
Connections between Relation Algebras and Cylindric Algebras Ian Hodkinson	27
Towards a Probabilistic Interpretation of Game Logic Ernst-Erich Doberkat	43

# **Theoretical Foundations**

Completeness and Incompleteness in Nominal Kleene Algebra Dexter Kozen, Konstantinos Mamouras, and Alexandra Silva	51
Closure, Properties and Closure Properties of Multirelations Rudolf Berghammer and Walter Guttmann	67
Relational Formalisations of Compositions and Liftings of Multirelations	84
Relations among Matrices over a Semiring Dylan Killingbeck, Milene Santos Teixeira, and Michael Winter	101
Completeness via Canonicity for Distributive Substructural Logics: A Coalgebraic Perspective Fredrik Dahlqvist and David Pym	119
Generalised N-ary Relations and Allegories Bartosz Zieliński	136
Mechanised Relation-Algebraic Order Theory in Ordered Categories without Meets	151
Reasoning about Computations and Programs	
Metaphorisms in Programming José N. Oliveira	171

Relational Mathematics for Relative Correctness Jules Desharnais, Nafi Diallo, Wided Ghardallou, Marcelo F. Frias, Ali Jaoua, and Ali Mili	191
Encoding and Decoding in Refinement Algebra	209
Type Checking by Domain Analysis in Ampersand Stef Joosten and Sebastiaan J.C. Joosten	225
Towards Interactive Verification of Programmable Logic Controllers Using Modal Kleene Algebra and KIV Roland Glück and Florian Benedikt Krebs	241
Investigating and Computing Bipartitions with Algebraic Means Rudolf Berghammer, Insa Stucke, and Michael Winter	257
Tool-Based Verification of a Relational Vertex Coloring Program Rudolf Berghammer, Peter Höfner, and Insa Stucke	275

# Applications of Relational and Algebraic Methods

L-Fuzzy Databases in Arrow Categories Evans Adjei, Wazed Chowdhury, and Michael Winter	295
Text Categorization Using Hyper Rectangular Keyword Extraction: Application to News Articles Classification Abdelaali Hassaine, Souad Mecheter, and Ali Jaoua	312
Solving a Tropical Optimization Problem via Matrix Sparsification Nikolai Krivulin	326
Towards Antichain Algebra Bernhard Möller	344
Decomposition of Database Preferences on the Power Set of the Domain <i>Patrick Roocks</i>	362
Roughness by Residuals: Algebraic Description of Rough Sets and an Algorithm for Finding Core Relations	380
Author Index	395